

8 次の関数を微分せよ。

(1) $y = (3x - 4)^5$

(2) $y = \log(3x - 4)$

(3) $y = e^{3x-4}$

(4) $y = \sin(3x - 4)$

(5) $y = \cos(3x - 4)$

(6) $y = \text{Sin}^{-1} \frac{x}{4}$

(7) $y = \text{Tan}^{-1} \frac{x}{4}$

(8) $y = x \log x$

(9) $y = \frac{e^{2x}}{x}$

(10) $y = x \sin 2x$

(11) $y = \frac{\sin 3x}{\cos 2x}$

(12) $y = e^{2x} \cos 3x$

(13) $y = \log(e^x + e^{-x})$

(14) $y = e^{\sin 2x}$

(15) $y = (\sin 2x + \cos 3x)^2$

8 次関数を微分せよ。

(1) $y = (3x - 4)^5$

$$y' = 5(3x - 4)^4 \times 3 = 15(3x - 4)^4$$

(2) $y = \log(3x - 4)$

$$y' = \frac{3}{3x - 4}$$

(3) $y = e^{3x-4}$

$$y' = 3e^{3x-4}$$

(4) $y = \sin(3x - 4)$

$$y' = 3\cos(3x - 4)$$

(5) $y = \cos(3x - 4)$

$$y' = -3\sin(3x - 4)$$

(6) $y = \text{Sin}^{-1} \frac{x}{4}$

$$y' = \frac{\frac{1}{4}}{\sqrt{1 - \left(\frac{x}{4}\right)^2}} = \frac{1}{\sqrt{16 - x^2}}$$

(7) $y = \text{Tan}^{-1} \frac{x}{4}$

$$y' = \frac{\frac{1}{4}}{\left(\frac{x}{4}\right)^2 + 1} = \frac{4}{x^2 + 16}$$

(8) $y = x \log x$

$$y' = 1 \times \log x + x \times \frac{1}{x} = 1 + \log x$$

(9) $y = \frac{e^{2x}}{x}$

$$y' = \frac{2e^{2x} \times x - e^{2x} \times 1}{x^2} = \frac{(2x - 1)e^{2x}}{x^2}$$

(10) $y = x \sin 2x$

$$y' = 1 \times \sin 2x + x \times 2 \cos 2x = \sin 2x + 2x \cos 2x$$

(11) $y = \frac{\sin 3x}{\cos 2x}$

$$y' = \frac{3 \cos 3x \times \cos 2x - \sin 3x \times (-2 \sin 2x)}{\cos^2 2x} = \frac{3 \cos 3x \cos 2x + 2 \sin 3x \sin 2x}{\cos^2 2x}$$

(12) $y = e^{2x} \cos 3x$

$$y' = 2e^{2x} \times \cos 3x + e^{2x} \times (-3 \sin 3x) = e^{2x} (2 \cos 3x - 3 \sin 3x)$$

(13) $y = \log(e^x + e^{-x})$

$$y' = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

(14) $y = e^{\sin 2x}$

$$y' = 2 \cos 2x \times e^{\sin 2x} = 2e^{\sin 2x} \cos 2x$$

(15) $y = (\sin 2x + \cos 3x)^2$

$$y' = 2(\sin 2x + \cos 3x)(2 \cos 2x - 3 \sin 3x)$$