

1 次の関数を微分せよ。

(1) $y = 5x^3 + 4\sqrt{x} + \frac{3}{x^2}$

$$y' = 15x^2 + \frac{2}{\sqrt{x}} - \frac{6}{x^3}$$

(2) $y = \sqrt[4]{3x+7}$

$$y' = \frac{3}{4\sqrt[4]{(3x+7)^3}}$$

(3) $y = x \sin 2x$

$$y' = \sin 2x + 2x \cos 2x$$

(4) $y = \log(1 + \sin x)$

$$y' = \frac{\cos x}{1 + \sin x}$$

(5) $y = (e^x + \log x)^3$

$$y' = 3(e^x + \log x)^2 \left(e^x + \frac{1}{x} \right)$$

(6) $y = \cos^5 x$

$$y' = -5 \sin x \cos^4 x$$

(7) $y = \frac{1 - \cos x}{1 + \cos x}$

$$y' = \frac{2 \sin x}{(1 + \cos x)^2}$$

(8) $y = (x^2 - x + 1)e^{3x}$

$$y' = (3x^2 - x + 2)e^{3x}$$

(9) $y = \text{Sin}^{-1} \frac{x}{4}$

$$y' = \frac{1}{\sqrt{16 - x^2}}$$

(10) $y = \text{Tan}^{-1} \frac{x}{4}$

$$y' = \frac{4}{x^2 + 16}$$

(11) $y = x \log x$

$$y' = 1 + \log x$$

(12) $y = \frac{e^{2x}}{x}$

$$y' = \frac{(2x-1)e^{2x}}{x^2}$$

(13) $y = e^{\sin 2x}$

$$y' = 2e^{\sin 2x} \cos 2x$$