

問 4.2 次の関数を微分せよ。

(1)  $y = x^5$

$$y' = 5x^4$$

(2)  $y = 3x^2 - 5x + 4$

$$y' = 6x - 5$$

(3)  $y = \frac{2}{x} = 2x^{-1}$

$$y' = -2x^{-2} = -\frac{2}{x^2}$$

(4)  $y = \frac{1}{3x^6} = \frac{1}{3}x^{-6}$

$$y' = -2x^{-7} = -\frac{2}{x^7}$$

(5)  $y = \sqrt[3]{x^4} = x^{\frac{4}{3}}$

$$y' = \frac{4}{3}x^{\frac{1}{3}} = \frac{4}{3}\sqrt[3]{x}$$

(6)  $y = \frac{1}{3}x^3 - \frac{1}{x} + 5\sqrt[5]{x} = \frac{1}{3}x^3 - x^{-1} + 5x^{\frac{1}{5}}$

$$y' = x^2 + x^{-2} + x^{-\frac{4}{5}} = x^2 + \frac{1}{x^2} + \frac{1}{\sqrt[5]{x^4}}$$

(7)  $y = (x^2 - 3x + 5)^3$

$$\begin{aligned} y' &= 3(x^2 - 3x + 5)^2 \times (2x - 3) \\ &= 3(2x - 3)(x^2 - 3x + 5)^2 \end{aligned}$$

(8)  $y = \frac{1}{(4x - 7)^6} = (4x - 7)^{-6}$

$$y' = -6(4x - 7)^{-7} \times 4 = -\frac{24}{(4x - 7)^7}$$

(9)  $y = \sqrt[3]{3x + 5} = (3x + 5)^{\frac{1}{3}}$

$$y' = \frac{1}{3}(3x + 5)^{-\frac{2}{3}} \times 3 = \frac{1}{\sqrt[3]{(3x + 5)^2}}$$

(10)  $y = \frac{2}{x + 1}$

$$y' = \frac{0 \times (x + 1) - 2 \times 1}{(x + 1)^2} = -\frac{2}{(x + 1)^2}$$

(11)  $y = \frac{4x + 3}{x - 2}$

$$\begin{aligned} y' &= \frac{4 \times (x - 2) - (4x + 3) \times 1}{(x - 2)^2} \\ &= \frac{(4x - 8) - (4x + 3)}{(x - 2)^2} = -\frac{11}{(x - 2)^2} \end{aligned}$$

(12)  $y = x^3(x - 1)^4$

$$\begin{aligned} y' &= 3x^2 \times (x - 1)^4 + x^3 \times \{4(x - 1)^3 \times 1\} \\ &= 3x^2(x - 1)^4 + 4x^3(x - 1)^3 \\ &= x^2(x - 1)^3 \{3(x - 1) + 4x\} \\ &= x^2(x - 1)^3(7x - 3) \end{aligned}$$